

Integrate Functions Given at Discrete Points: Trapezoidal Rule with Unequal Segments



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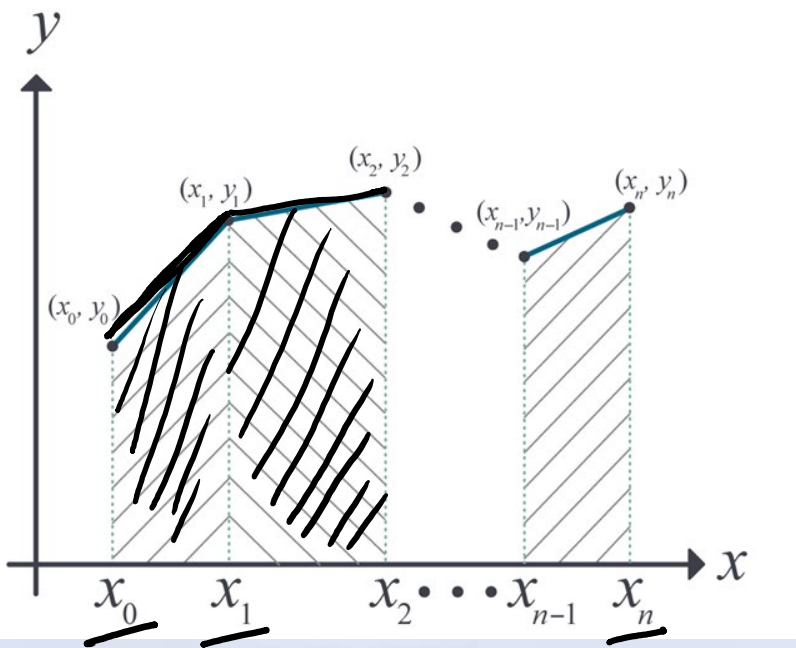
Transforming Numerical Methods Education for STEM Undergraduates



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- Click on Integrating Functions Given at Discrete Points





$$\begin{aligned}
 & x_n \\
 & \int_{x_0}^{x_n} f(x) dx \\
 & = \int_{x_0}^{x_1} f(x) dx + \dots + \int_{x_{n-1}}^{x_n} f(x) dx
 \end{aligned}$$

$$\approx \underbrace{(x_1 - x_0) \left(\frac{f(x_0) + f(x_1)}{2} \right)} + \dots + \underbrace{(x_n - x_{n-1}) \left(\frac{f(x_{n-1}) + f(x_n)}{2} \right)}$$

$$= \sum_{i=1}^n (x_i - x_{i-1}) \left(\frac{f(x_{i-1}) + f(x_i)}{2} \right)$$



The upward velocity of a rocket is given as a function of time in the table. Using the trapezoidal rule with unequal segments, determine the displacement s of the rocket from $t = 11$ to $t = 16$ seconds.

$t(s)$	$v(t)(m/s)$
0	0
10	227.04 ✓
15	362.78 ✓
20	517.35 ✓
22.5	602.97
30	901.67

$$\begin{aligned}
 s &= \int_{11}^{16} v(t) dt \\
 &= \int_{11}^{15} v(t) dt + \int_{15}^{16} v(t) dt \\
 &\approx (15-11) \left(\frac{v(15) + v(11)}{2} \right) \\
 &\quad + (16-15) \left(\frac{v(15) + v(16)}{2} \right)
 \end{aligned}$$



$$v(t) = v_0 + \frac{v_1 - v_0}{t_1 - t_0} (t - t_0), \quad t_0 \leq t \leq t_1$$

$$v(t) = v(10) + \frac{v(15) - v(10)}{15 - 10} (t - 10), \quad 10 \leq t \leq 15$$

$$v(11) = 227.04 + \frac{362.78 - 227.04}{15 - 10} (11 - 10)$$

$$= 254.19 \text{ m/s}$$



$$v(t) = v(15) + \frac{v(20) - v(15)}{20 - 15} (t - 15)$$

$15 \leq t \leq 20$

$$v(16) = 362.78 + \frac{517.35 - 362.78}{20 - 15} (16 - 15)$$

$$= 393.69 \text{ m/s}$$



$$\int_{11}^{16} v(t) dt \approx \frac{15-11}{2} (v(11)^{\times} + v(15)^{\checkmark}) \\ + \frac{16-15}{2} (v(15)^{\checkmark} + v(16)^{\times})$$

$$= \frac{15-11}{2} (254.19 + 362.78) \\ + \frac{16-15}{2} (362.78 + 393.69)$$

$$= 1612.2 \text{ m}$$

END



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Acknowledgement

This instructional resource is brought to you by
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This material is based upon work supported by the National Science Foundation under Grant #2013271 (Transforming Undergraduate Engineering Education through Adaptive Learning and Student Data Analytics). Any opinions, findings, and conclusions or recommendations expressed in this material are those of the author(s) and do not necessarily reflect the views of the National Science Foundation.





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