

Holistic Numerical Methods Institute
committed to bringing numerical methods to undergraduates

Multiple-Choice Test Background Simultaneous Linear Equations

1. Given $[A] = \begin{bmatrix} 6 & 2 & 3 & 9 \\ 0 & 1 & 2 & 3 \\ 0 & 0 & 4 & 5 \\ 0 & 0 & 0 & 6 \end{bmatrix}$ then $[A]$ is a _____ matrix.

- (A) diagonal
- (B) identity
- (C) lower triangular
- (D) upper triangular

2. A square matrix $[A]$ is lower triangular if

- (A) $a_{ij} = 0, j > i$
- (B) $a_{ij} = 0, i > j$
- (C) $a_{ij} \neq 0, i > j$
- (D) $a_{ij} \neq 0, j > i$

3. Given

$$[A] = \begin{bmatrix} 12.3 & -12.3 & 20.3 \\ 11.3 & -10.3 & -11.3 \\ 10.3 & -11.3 & -12.3 \end{bmatrix}, [B] = \begin{bmatrix} 2 & 4 \\ -5 & 6 \\ 11 & -20 \end{bmatrix}$$

then if

$$[C] = [A] [B], \text{ then}$$

$$c_{31} = \underline{\hspace{2cm}}$$

- (A) -58.2
- (B) -37.6
- (C) 219.4
- (D) 259.4

MULTIPLE CHOICE TEST – BACKGROUND: SIMULTANEOUS LINEAR EQUATIONS

4. The following system of equations has _____ solution(s).

$$\begin{aligned}x + y &= 2 \\ 6x + 6y &= 12\end{aligned}$$

- (A) infinite
- (B) no
- (C) two
- (D) unique

5. Consider there are only two computer companies in a country. The companies are named *Dude* and *Imac*. Each year, company *Dude* keeps $1/5^{\text{th}}$ of its customers, while the rest switch to *Imac*. Each year, *Imac* keeps $1/3^{\text{rd}}$ of its customers, while the rest switch to *Dude*. If in 2003, *Dude* had $1/6^{\text{th}}$ of the market and *Imac* had $5/6^{\text{th}}$ of the market, what will be share of *Dude* computers when the market becomes stable?

- (A) 37/90
- (B) 5/11
- (C) 6/11
- (D) 53/90

6. Three kids - Jim, Corey and David receive an inheritance of \$2,253,453. The money is put in three trusts but is not divided equally to begin with. Corey's trust is three times that of David's because Corey made an *A* in Dr. Kaw's class. Each trust is put in an interest generating investment. The three trusts of Jim, Corey and David pays an interest of 6%, 8%, 11%, respectively. The total interest of all the three trusts combined at the end of the first year is \$190,740.57. The equations to find the trust money of Jim (*J*), Corey (*C*) and David (*D*) in a matrix form is

$$(A) \begin{bmatrix} 1 & 1 & 1 \\ 0 & 3 & -1 \\ 0.06 & 0.08 & 0.11 \end{bmatrix} \begin{bmatrix} J \\ C \\ D \end{bmatrix} = \begin{bmatrix} 2,253,453 \\ 0 \\ 190,740.57 \end{bmatrix}$$

$$(B) \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & -3 \\ 0.06 & 0.08 & 0.11 \end{bmatrix} \begin{bmatrix} J \\ C \\ D \end{bmatrix} = \begin{bmatrix} 2,253,453 \\ 0 \\ 190,740.57 \end{bmatrix}$$

$$(C) \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & -3 \\ 6 & 8 & 11 \end{bmatrix} \begin{bmatrix} J \\ C \\ D \end{bmatrix} = \begin{bmatrix} 2,253,453 \\ 0 \\ 190,740.57 \end{bmatrix}$$

$$(D) \begin{bmatrix} 1 & 1 & 1 \\ 0 & 3 & -1 \\ 6 & 8 & 11 \end{bmatrix} \begin{bmatrix} J \\ C \\ D \end{bmatrix} = \begin{bmatrix} 2,253,453 \\ 0 \\ 19,074,057 \end{bmatrix}$$