

Holistic Numerical Methods Institute
committed to bringing numerical methods to undergraduates

Multiple-Choice Test
Nonlinear Regression
Regression

1. When using the linearized data model to find the constants of the regression model $y = ae^{bx}$ to best fit $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$, the sum of the squares of the residuals that is minimized is

- (A) $\sum_{i=1}^n (y_i - ae^{bx_i})^2$
- (B) $\sum_{i=1}^n (\ln(y_i) - \ln a - bx_i)^2$
- (C) $\sum_{i=1}^n (y_i - \ln a - bx_i)^2$
- (D) $\sum_{i=1}^n (\ln(y_i) - \ln a - b \ln(x_i))^2$

2. It is suspected from theoretical considerations that the rate of flow from a firehouse is proportional to some power of the nozzle pressure. Assume pressure data is more accurate. You are linearizing the data.

Flow rate, F (gallons/min)	96	129	135	145	168	235
Pressure, p (psi)	11	17	20	25	40	55

The exponent of the power of the nozzle pressure in the regression model, $F = ap^b$ most nearly is

- (A) 0.497
(B) 0.556
(C) 0.578
(D) 0.678

3. The linearized data model for the stress-strain curve $\sigma = K_1 \varepsilon^{-K_2 \varepsilon}$ for concrete in compression, where σ is the stress and ε is the strain is

- (A) $\ln \sigma = \ln k_1 + \ln \varepsilon - k_2 \varepsilon$
- (B) $\ln \frac{\sigma}{\varepsilon} = \ln k_1 - k_2 \varepsilon$
- (C) $\ln \frac{\sigma}{\varepsilon} = \ln k_1 + k_2 \varepsilon$
- (D) $\ln \sigma = \ln(k_1 \varepsilon) - k_2 \varepsilon$

4. In nonlinear regression, finding the constants of the model requires solution of simultaneous nonlinear equations. However in the exponential model, $y = ae^{bx}$ that is best fit to $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$, the value of b can be found as a solution of a sample nonlinear equation. That equation is given by

- (A) $\sum_{i=1}^n y_i x_i e^{bx_i} - \sum_{i=1}^n y_i e^{bx_i} \sum_{i=1}^n x_i = 0$
- (B) $\sum_{i=1}^n y_i x_i e^{bx_i} - \frac{\sum_{i=1}^n y_i e^{bx_i}}{\sum_{i=1}^n e^{2bx_i}} \sum_{i=1}^n x_i e^{2bx_i} = 0$
- (C) $\sum_{i=1}^n y_i x_i e^{bx_i} - \frac{\sum_{i=1}^n y_i e^{bx_i}}{\sum_{i=1}^n e^{2bx_i}} \sum_{i=1}^n e^{bx_i} = 0$
- (D) $\sum_{i=1}^n y_i e^{bx_i} - \frac{\sum_{i=1}^n y_i e^{bx_i}}{\sum_{i=1}^n e^{2bx_i}} \sum_{i=1}^n x_i e^{2bx_i} = 0$

5. There is a functional relationship between the mass density ρ of air and altitude h above the sea level

Altitude above sea level, h (km)	0.32	0.64	1.28	1.60
Mass Density, ρ (kg/m ³)	1.15	1.10	1.05	0.95

In the regression model $\rho = k_1 e^{-k_2 h}$, the constant k_2 is found as $k_2 = 0.1315$. Assuming the mass density of air at the top of the atmosphere is $1/1000^{\text{th}}$ of the mass density of air at sea level. The altitude in km of the top of the atmosphere most nearly is

- (A) 46.2
- (B) 46.6
- (C) 49.7
- (D) 52.5

6. A steel cylinder at 80°F of length 12" is placed in a liquid nitrogen bath (-315°F). If thermal expansion coefficient of steel behaves as a second order polynomial of temperature and the polynomial is found by regressing the data below,

Temperature ($^\circ\text{F}$)	Thermal expansion coefficient (μ in/in/ $^\circ\text{F}$)
-320	2.76
-240	3.83
-160	4.72
-80	5.43
0	6.00
80	6.47

the reduction in the length of cylinder most nearly is

- (A) 0.0219"
- (B) 0.0231"
- (C) 0.0235"
- (D) 0.0307"