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% Topic : Newton-Raphson Method - Roots of Equations
% Simulation : Simulation of the Method
% Language : Matlab r12
% Authors : Nathan Collier, Autar Kaw
% Date : 21 August 2002
% Abstract : This simulation illustrates the Newton-Raphson method of
% finding roots of an equation  $f(x)=0$ .
%
clear all
% INPUTS: Enter the following
% Function in  $f(x)=0$ 
syms x
f = x^3-0.165*x^2+3.993*10^(-4);
% Initial guess
x0 = 0.05;
% Lower bound of range of 'x' to be seen
lrange = -0.02;
% Upper bound of range of 'x' to be seen
urange = 0.12;
%
% SOLUTION
g=diff(f);
% The following finds the upper and lower 'y' limits for the plot based on the given
% 'x' range in the input section.
maxi = subs(f,x,lrange);
mini = subs(f,x,lrange);
for i=lrange:(urange-lrange)/10:urange
    if subs(f,x,i) > maxi
        maxi = subs(f,x,i);
    end
    if subs(f,x,i) < mini
        mini = subs(f,x,i);
    end
end
end
tot=maxi-mini;
mini=mini-0.1*tot;
maxi=maxi+0.1*tot;

% This calculates window size to be used in figures
set(0,'Units','pixels')
scnsize = get(0,'ScreenSize');
wid = round(scnsize(3));
hei = round(0.95*scnsize(4));
wind = [1, 1, wid, hei];

% This graphs the function and the line representing the initial guess

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figure('Position',wind)
clf
ezplot(f,[lrange,urange])
hold on
plot([x0,x0],[maxi,mini],'g','linewidth',2)
plot([lrange,urange],[0,0],'k','linewidth',1)
title('Entered function on given interval with initial guess')
hold off

% -----
% Iteration 1
figure('Position',wind)
x1=x0-subst(f,x,x0)/subst(g,x,x0);
ea=abs((x1-x0)/x1)*100;
m=-subst(f,x,x0)/(x1-x0);
b=subst(f,x,x0)*(1+x0/(x1-x0));
lefty=(maxi-b)/m;
righty=(mini-b)/m;
% This graphs the function and two lines representing the two guesses
clf
subplot(2,1,2),ezplot(f,[lrange urange])
hold on
plot([x0,x0],[maxi,mini],'g','linewidth',2)
plot([x1,x1],[maxi,mini],'g','linewidth',2)
plot([lefty,righty],[maxi,mini],'r','linewidth',2)
plot([lrange,urange],[0,0],'k','linewidth',1)
title('Entered function on given interval with current and next root and tangent line of the
curve at the current root')

% This portion adds the text and math to the top part of the figure window
subplot(2,1,1), text(0,1,['Iteration 1'])
text(0.1,.8,['x1 = x0 - (f(x0)/g(x0)) = ',num2str(x1)])
text(0,.4,['Absolute relative approximate error'])
text(0.1,.2,['ea = abs((x1 - x0) / x1)*100 = ',num2str(ea),'%'])
axis off
hold off

% -----
% Iteration 2
figure('Position',wind)
x2=x1-subst(f,x,x1)/subst(g,x,x1);
ea=abs((x2-x1)/x2)*100;
m=-subst(f,x,x1)/(x2-x1);
b=subst(f,x,x1)*(1+x1/(x2-x1));
lefty=(maxi-b)/m;
righty=(mini-b)/m;

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% This graphs the function and two lines representing the two guesses
clf
subplot(2,1,2),ezplot(f,[lrange,urange])
hold on
plot([x1,x1],[maxi,mini],'g','linewidth',2)
plot([x2,x2],[maxi,mini],'g','linewidth',2)
plot([lefty,righty],[maxi,mini],'r','linewidth',2)
plot([lrange,urange],[0,0],'k','linewidth',1)
title('Entered function on given interval with current and next root and tangent line of the
curve at the current root')

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% Calculate relative approximate error
ea=abs((x2-x1)/x2)*100;

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% This portion adds the text and math to the bottom part of the figure window
subplot(2,1,1), text(0,1,['Iteration 2'])
text(0.1,.8,['x2 = x1 - (f(x1)/g(x1)) = ',num2str(x1)])
text(0,.4,['Absolute relative approximate error'])
text(0.1,.2,['ea = abs((x2 - x1) / x2)*100 = ',num2str(ea),'%'])
axis off

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% -----

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% Iteration 3

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figure('Position',wind)

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x3=x2-subst(f,x,x2)/subst(g,x,x2);

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ea=abs((x3-x2)/x3)*100;

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m=-subst(f,x,x2)/(x3-x2);

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b=subst(f,x,x2)*(1+x2/(x3-x2));

```

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lefty=(maxi-b)/m;

```

```

righty=(mini-b)/m;

```

```

% This graphs the function and two lines representing the two guesses

```

```

clf

```

```

subplot(2,1,2),ezplot(f,[lrange,urange])

```

```

hold on

```

```

plot([x2,x2],[maxi,mini],'g','linewidth',2)

```

```

plot([x3,x3],[maxi,mini],'g','linewidth',2)

```

```

plot([lefty,righty],[maxi,mini],'r','linewidth',2)

```

```

plot([lrange,urange],[0,0],'k','linewidth',1)

```

```

title('Entered function on given interval with current and next root and tangent line of the
curve at the current root')

```

```

% Calculate relative approximate error

```

```

ea=abs((x2-x1)/x2)*100;

```

```

% This portion adds the text and math to the bottom part of the figure window

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subplot(2,1,1), text(0,1,['Iteration 3'])

```

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text(0.1,.8,['x3 = x2 - (f(x2)/g(x2)) = ',num2str(x3)])
text(0.4,['Absolute relative approximate error'])
text(0.1,.2,['ea = abs((x3 - x2) / x3)*100 = ',num2str(ea),'%'])
axis off
```







