

Topic : Newton Raphson Method - Roots of Equations

Simulation : Graphical Simulation of the Method

Language : Mathematica 4.1

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Date : 11 July 2002

Abstract : This simulation illustrates the Newton-Raphson method of finding the root of an equation $f[x] = 0$.

■ **INPUTS: Enter the Following**

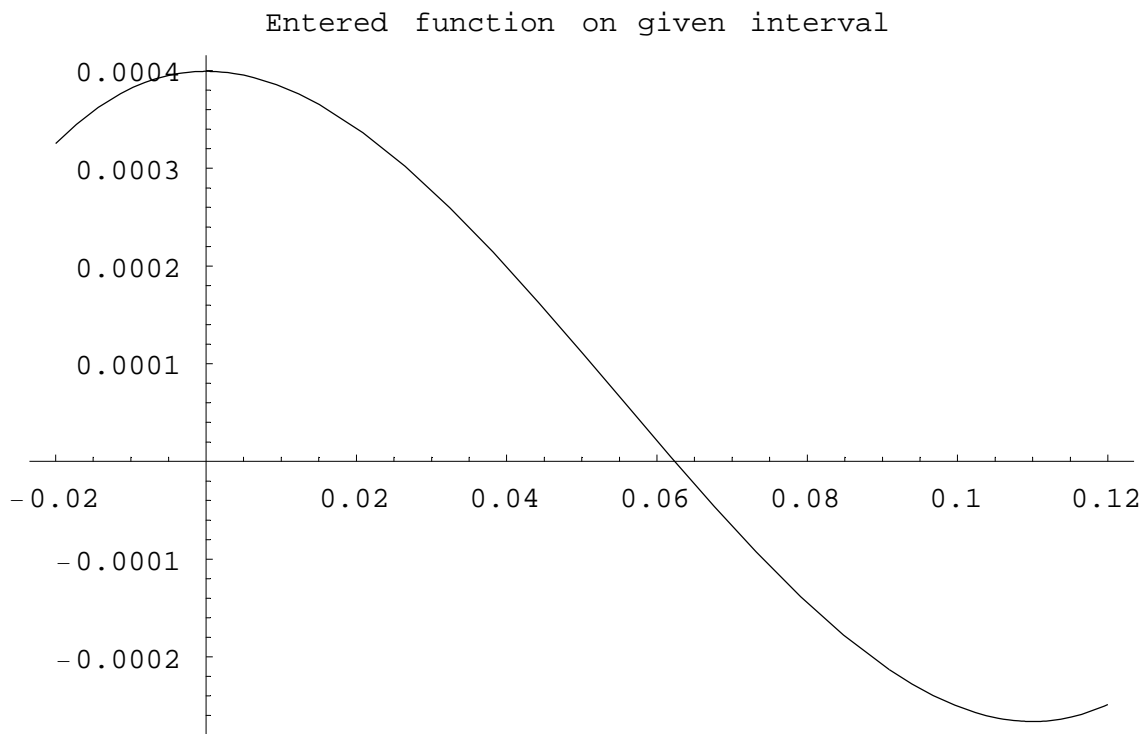
Function in $f[x] = 0$

```
In[403]:= f[x_] := x^3 - 0.165 * x^2 + 3.993 * 10^-4
```

Range of 'x' you want to see the function

```
In[404]:= xbegin = -0.02;  
xend = 0.12;
```

```
In[406]:= curve = Plot[f[x], {x, xbegin, xend}, PlotLabel ->  
"Entered function on given interval", TextStyle -> {FontSize -> 11}];
```



Initial guess

```
In[407]:= x0 = 0.05;
```

Because this method uses a line tangent to the function at the initial guess, we must calculate the derivative of the function to find the slope of the line at this point. Here we will define the derivative of the function $f(x)$ as $g(x)$.

```
In[408]:= g[x_] := f'[x]
```

```
In[409]:= maxi = f[x_begin];
mini = f[x_begin];
step = (x_end - x_begin) / 10;
Do[ If[f[i] > maxi, maxi = f[i]];
  If[f[i] < mini, mini = f[i]], {i, x_begin, x_end, step}];
tot = maxi - mini;
mini = mini - 0.1 * tot;
maxi = maxi + 0.1 * tot;
```

Iteration 1

```
In[416]:= x1 = x0 - f[x0] / g[x0]
```

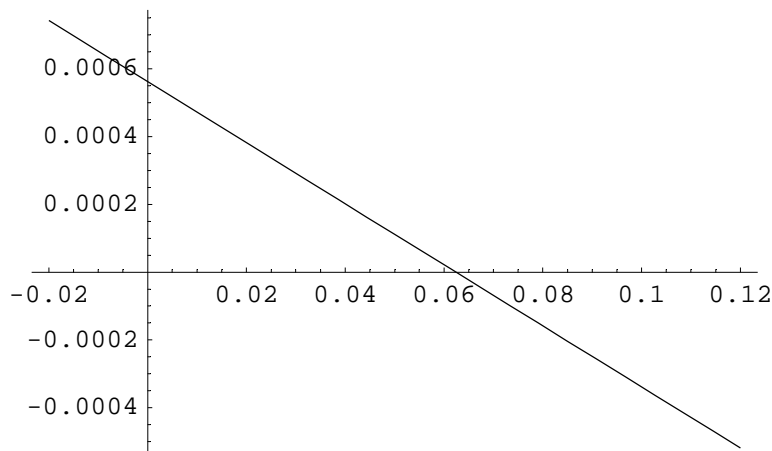
```
Out[416]= 0.0624222
```

```
In[417]:= εa = Abs[(x1 - x0) / x1 * 100]
```

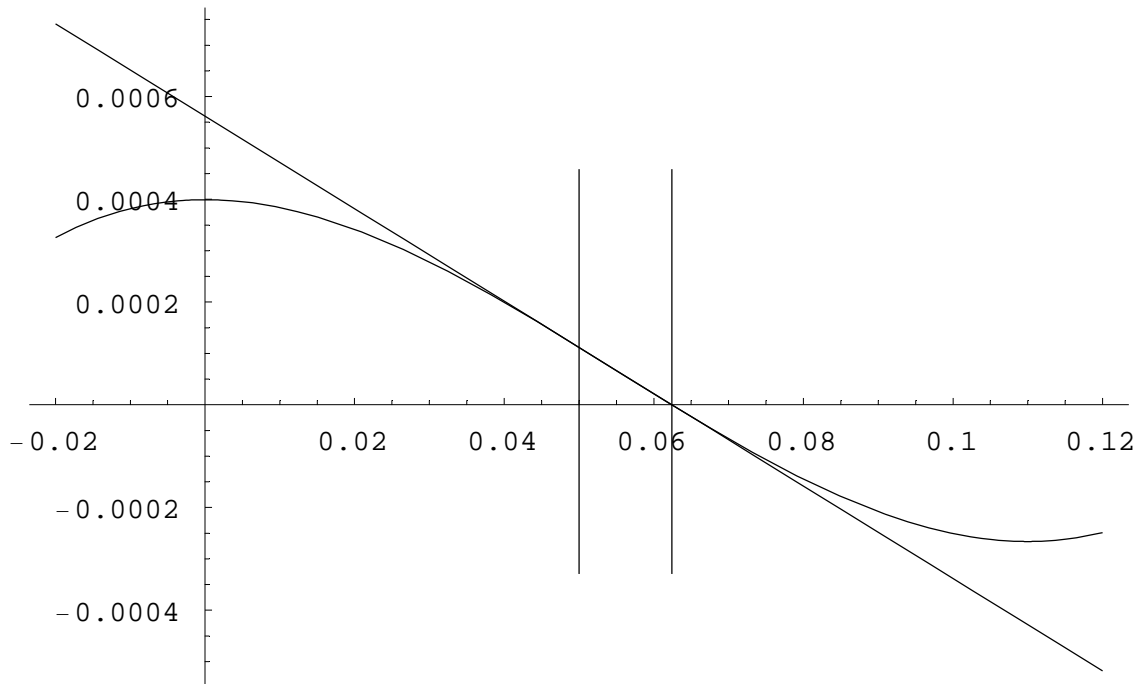
```
Out[417]= 19.9003
```

```
In[418]:= tanline[x_] := f[x0] + ((0 - f[x0]) / (x1 - x0)) * (x - x0)
```

```
In[419]:= tline = Plot[tanline[x], {x, x_begin, x_end}];
```



```
In[420]:= Show[Graphics[Line[{{x0, maxi}, {x0, mini}}]], curve,
Graphics[Line[{{x1, maxi}, {x1, mini}}]], tline, Axes → True,
PlotLabel → "Entered function on given interval with upper and
lower guesses and estimated root", TextStyle → {FontSize → 11}];
unction on given interval with upper and lower guesses and estimated
```



Iteration 2

```
In[421]:= x2 = x1 - f[x1] / g[x1]
```

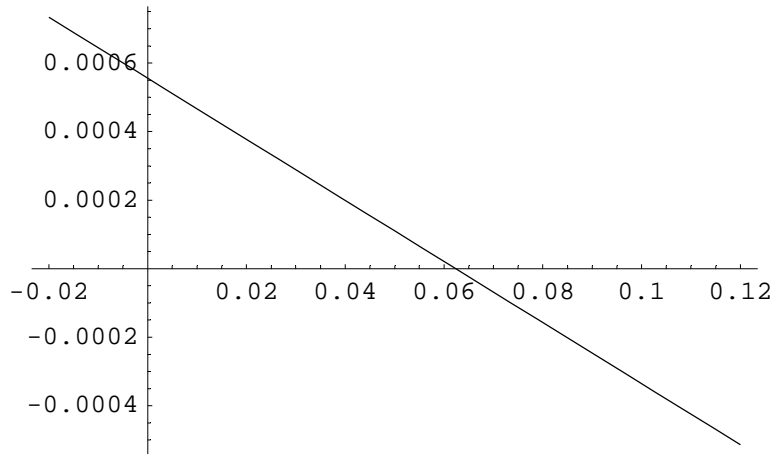
```
Out[421]= 0.0623776
```

```
In[422]:= εa = Abs[(x2 - x1) / x2 * 100]
```

```
Out[422]= 0.0715733
```

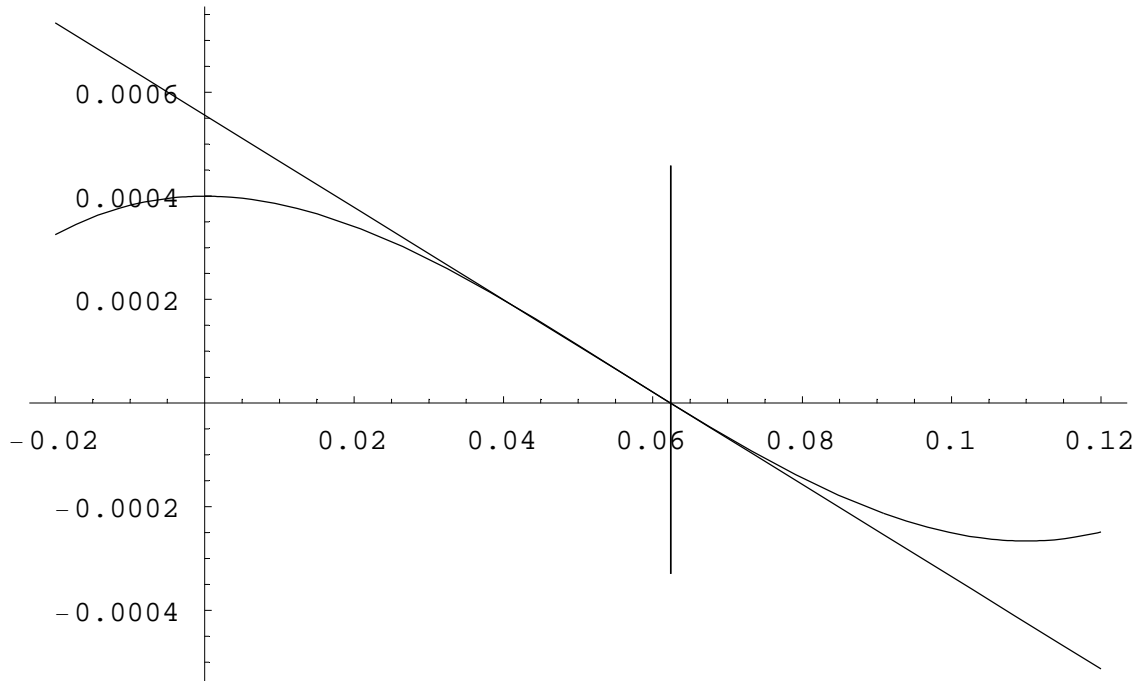
```
In[423]:= tanline[x_] := f[x1] + ((0 - f[x1]) / (x2 - x1)) * (x - x1)
```

```
In[424]:= tline = Plot[tanline[x], {x, xbegin, xend}];
```



```
In[425]:= Show[Graphics[Line[{{x1, maxi}, {x1, mini}}]], curve,
Graphics[Line[{{x2, maxi}, {x2, mini}}]], tline, Axes → True,
PlotLabel → "Entered function on given interval with upper and
lower guesses and estimated root", TextStyle → {FontSize → 11}];
```

unction on given interval with upper and lower guesses and estimated



Iteration 3

```
In[426]:= x3 = x2 - f[x2] / g[x2]
```

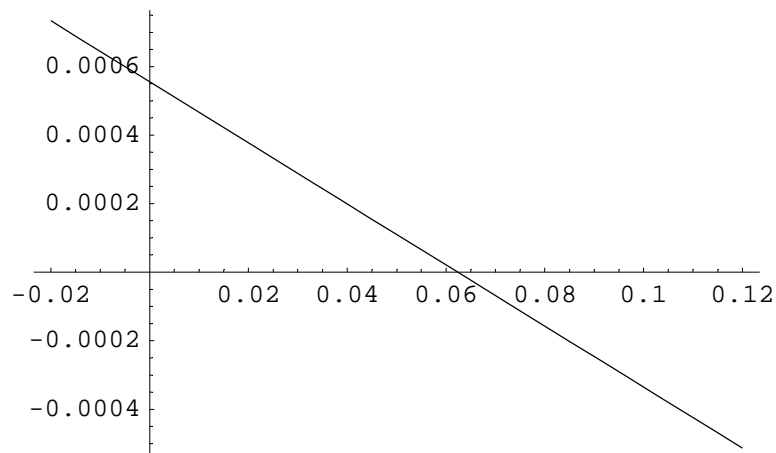
```
Out[426]= 0.0623776
```

```
In[427]:= εa = Abs[(x3 - x2) / x3 * 100]
```

```
Out[427]= 7.96806 × 10-6
```

```
In[428]:= tanline[x_] := f[x2] + ((0 - f[x2]) / (x3 - x2)) * (x - x2)
```

```
In[429]:= tline = Plot[tanline[x], {x, xbegin, xend};
```



```
In[430]:= Show[Graphics[Line[{{x3, maxi}, {x3, mini}}]], curve,  
Graphics[Line[{{x2, maxi}, {x2, mini}}]], tline, Axes → True,  
PlotLabel → "Entered function on given interval with upper and  
lower guesses and estimated root", TextStyle → {FontSize → 11}];  
unction on given interval with upper and lower guesses and estimated
```

